

# Package ‘NetworkInference’

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**Type** Package

**Title** Inferring Latent Diffusion Networks

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**Description** This is an R implementation of the netinf algorithm (Gomez Rodriguez, Leskovec, and Krause, 2010)<[doi:10.1145/1835804.1835933](https://doi.org/10.1145/1835804.1835933)>. Given a set of events that spread between a set of nodes the algorithm infers the most likely stable diffusion network that is underlying the diffusion process.

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**Imports** Rcpp (>= 0.12.5), assertthat, checkmate, ggplot2, ggrepel, stats

**LinkingTo** Rcpp, RcppProgress

**BugReports** <https://github.com/desmarais-lab/NetworkInference/issues>

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**VignetteBuilder** knitr

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## Contents

as.data.frame.cascade . . . . .	2
as.matrix.cascade . . . . .	3

as_cascade_long . . . . .	4
as_cascade_wide . . . . .	5
ascades . . . . .	6
count_possible_edges . . . . .	6
drop_nodes . . . . .	7
is.cascade . . . . .	8
is.diffnet . . . . .	8
netinf . . . . .	9
NetworkInference . . . . .	10
plot.cascade . . . . .	11
plot.diffnet . . . . .	12
policies . . . . .	13
simulate_cascades . . . . .	14
simulate_rnd_cascades . . . . .	15
sim_validation . . . . .	16
subset_cascade . . . . .	17
subset_cascade_time . . . . .	17
summary.cascade . . . . .	18
validation . . . . .	19
<b>Index</b>	<b>20</b>

---

as.data.frame.cascade *Convert a cascade object to a data frame*

---

## Description

Generates a data frame containing the cascade information in the cascade object.

## Usage

```
## S3 method for class 'cascade'
as.data.frame(x, row.names = NULL, optional = FALSE,
  ...)
```

## Arguments

x	Cascade object to convert.
row.names	NULL or a character vector giving the row names for the data frame. Missing values are not allowed.
optional	logical. If TRUE, setting row names and converting column names (to syntactic names: see <code>make.names</code> ) is optional. (Not supported)
...	Additional arguments passed to <code>data.frame</code> .

**Value**

A data frame with three columns. Containing 1) The names of the nodes ("node\_name") that experience an event in each cascade, 2) the event time ("event\_time") of the corresponding node, 3) the cascade identifier "cascade\_id".

**Examples**

```
data(cascades)
as.data.frame(cascades)
```

---

as.matrix.cascade	<i>Convert a cascade object to a matrix</i>
-------------------	---

---

**Description**

Generates a [matrix](#) containing the cascade information in the cascade object in wide format. Missing values are used for nodes that do not experience an event in a cascade.

**Usage**

```
## S3 method for class 'cascade'
as.matrix(x, ...)
```

**Arguments**

x	cascade object to convert.
...	additional arguments to be passed to or from methods. (Currently not supported.)

**Value**

A matrix containing all cascade information in wide format. That is, each row of the matrix corresponds to a node and each column to a cascade. Cell entries are event times. Censored nodes have NA for their entry.

**Examples**

```
data(cascades)
as.matrix(cascades)
```

---

as_cascade_long	<i>Transform long data to cascade</i>
-----------------	---------------------------------------

---

### Description

Create a cascade object from data in long format.

### Usage

```
as_cascade_long(data, cascade_node_name = "node_name",
  event_time = "event_time", cascade_id = "cascade_id",
  node_names = NULL)
```

### Arguments

data	<a href="#">data.frame</a> , containing the cascade data with column names corresponding to the arguments provided to cascade_node_names, event_time and cascade_id.
cascade_node_name	character, column name of data that specifies the node names in the cascade.
event_time	character, column name of data that specifies the event times for each node involved in a cascade.
cascade_id	character, column name of the cascade identifier.
node_names	character, factor or numeric vector containing the names for each node. Optional. If not provided, node names are inferred from the cascade data.

### Details

Each row of the data describes one event in the cascade. The data must contain at least three columns:

1. Cascade node name: The identifier of the node that experiences the event.
2. Event time: The time when the node experiences the event. Note that if the time column is of class date or any other special time class, it will be converted to an integer with 'as.numeric()'.
3. Cascade id: The identifier of the cascade that the event pertains to.

The default names for these columns are node\_name, event\_time and cascade\_id. If other names are used in the data object the names have to be specified in the corresponding arguments (see argument documentation)

### Value

An object of class cascade. This is a list containing three (named) elements:

1. "node\_names" A character vector of node names.
2. "cascade\_nodes" A list with one character vector per cascade containing the node names in order of the events.
3. "cascade\_times" A list with one element per cascade containing the event times for the nodes in "cascade\_names".

**Examples**

```
df <- simulate_rnd_cascades(10, n_nodes = 20)
cascades <- as_cascade_long(df)
is.cascade(cascades)
```

---

as_cascade_wide	<i>Transform wide data to cascade</i>
-----------------	---------------------------------------

---

**Description**

Create a cascade object from data in wide format.

**Usage**

```
as_cascade_wide(data, node_names = NULL)
```

**Arguments**

data	<a href="#">data.frame</a> or <a href="#">matrix</a> , rows corresponding to nodes, columns to cascades. Matrix entries are the event times for each node, cascade pair. Missing values indicate censored observations, that is, nodes that did not have an event). Specify column and row names if cascade and node ids other than integer sequences are desired. Note that, if the time column is of class date or any other special time class, it will be converted to an integer with ‘as.numeric()’.
node_names	character, factor or numeric vector, containing names for each node. Optional. If not provided, node names are inferred from the provided data.

**Details**

If data is in wide format, each row corresponds to a node and each column to a cascade. Each cell indicates the event time for a node - cascade combination. If a node did not experience an event for a cascade (the node is censored) the cell entry must be NA.

**Value**

An object of class cascade. This is a list containing three (named) elements:

1. "node\_names" A character vector of node names.
2. "cascade\_nodes" A list with one character vector per cascade containing the node names in order of the events.
3. "cascade\_times" A list with one element per cascade containing the event times for the nodes in "cascade\_names".

**Examples**

```
data("policies")
cascades <- as_cascade_long(policies, cascade_node_name = 'statenam',
                           event_time = 'adopt_year', cascade_id = 'policy')
wide_policies = as.matrix(cascades)
cascades <- as_cascade_wide(wide_policies)
is.cascade(cascades)
```

---

cascades	<i>Example cascades</i>
----------	-------------------------

---

**Description**

An example dataset of 31 nodes and 54 cascades. From the original netinf implementation in SNAP.

**Usage**

```
data(cascades)
```

**Format**

An object of class cascade containing 4 objects

**node\_names** Character node names

**cascade\_nodes** A list of integer vectors. Each containing the names of the nodes infected in this cascades in the order of infection

**cascade\_times** A list of numeric vectors. Each containing the infection times for the corresponding nodes in cascade\_nodes

**Source**

<https://github.com/snap-stanford/snap/blob/master/examples/netinf/example-cascades.txt>

---

count_possible_edges	<i>Count the number of possible edges in the dataset</i>
----------------------	--

---

**Description**

Across all cascades, count the edges that are possible. An edge from node  $u$  to node  $v$  is only possible if in at least one cascade  $u$  experienced an event before  $v$ .

**Usage**

```
count_possible_edges(cascades)
```

**Arguments**

cascades            Object of class cascade containing the data.

**Value**

An integer count.

**Examples**

```
data(cascades)
count_possible_edges(cascades)
```

---

drop_nodes	<i>Drop nodes from a cascade object</i>
------------	---

---

**Description**

Drop nodes from a cascade object

**Usage**

```
drop_nodes(cascades, nodes, drop = TRUE)
```

**Arguments**

cascades            cascade, object to drop nodes from.  
nodes                character or integer, vector of node\_ids to drop.  
drop                 logical, Should empty cascades be dropped.

**Value**

An object of class cascade containing the cascades without the dropped nodes.

**Examples**

```
data(policies)
cascades <- as_cascade_long(policies, cascade_node_name = 'statenam',
                           event_time = 'adopt_year', cascade_id = 'policy')
new_cascades <- drop_nodes(cascades, c("California", "New York"))
```

---

is.cascade	<i>Is the object of class cascade?</i>
------------	--

---

**Description**

Is the object of class cascade?

**Usage**

```
is.cascade(object)
```

**Arguments**

object            the object to be tested.

**Value**

TRUE if object is a cascade, FALSE otherwise.

**Examples**

```
data(cascades)
is.cascade(cascades)
# > TRUE
is.cascade(1)
# > FALSE
```

---

is.diffnet	<i>Is the object of class diffnet?</i>
------------	--

---

**Description**

Tests if an object is of class diffnet. The class diffnet is appended to the object returned by [netinf](#) for dispatch of appropriate plotting methods.

**Usage**

```
is.diffnet(object)
```

**Arguments**

object            the object to be tested.

**Value**

TRUE if object is a diffnet, FALSE otherwise.



**Examples**

```
data(cascades)
result <- netinf(cascades, n_edges = 6, params = 1)
is.diffnet(result)
```

---

netinf

*Infer latent diffusion network*


---

**Description**

Infer a network of diffusion ties from a set of cascades. Each cascade is defined by pairs of node ids and infection times.

**Usage**

```
netinf(cascades, trans_mod = "exponential", n_edges = NULL,
       p_value_cutoff = NULL, params = NULL, quiet = FALSE,
       trees = FALSE)
```

**Arguments**

cascades	an object of class cascade containing node and cascade information. See <a href="#">as_cascade_long</a> and <a href="#">as_cascade_wide</a> for details.
trans_mod	character, indicating the choice of model: "exponential", "rayleigh" or "log-normal".
n_edges	integer, number of edges to infer. Leave unspecified if using p_value_cutoff.
p_value_cutoff	numeric, in the interval (0, 1). If specified, edges are inferred in each iteration until the Vuong test for edge addition reaches the p-value cutoff or when the maximum possible number of edges is reached. Leave unspecified if using n_edges to explicitly specify number of edges to infer.
params	numeric, Parameters for diffusion model. If left unspecified reasonable parameters are inferred from the data. See details for how to specify parameters for the different distributions.
quiet	logical, Should output on progress be suppressed.
trees	logical, Should the inferred cascade trees be returned. Note, that this will lead to a different the structure of the function output. See section Value for details.

**Details**

The algorithm is describe in detail in Gomez-Rodriguez et al. (2010). Additional information can be found on the netinf website (<http://snap.stanford.edu/netinf/>).

- Exponential distribution: trans\_mod = "exponential", params = c(lambda). Parametrization:  $\lambda e^{-\lambda x}$ .
- Rayleigh distribution: trans\_mod = "rayleigh", params = c(alpha). Parametrization:  $\frac{x}{\alpha^2} e^{-\frac{x^2}{2\alpha^2}}$ .

- Log-normal distribution: `trans_mod = "log-normal"`, `params = c(mu, sigma)`. Parametrization:  $\frac{1}{x\sigma\sqrt{2\pi}}e^{-\frac{(\ln x - \mu)^2}{2\sigma^2}}$ .

If higher performance is required and for very large data sets, a faster pure C++ implementation is available in the Stanford Network Analysis Project (SNAP). The software can be downloaded at <http://snap.stanford.edu/netinf/>.

## Value

Returns the inferred diffusion network as an edgelist in an object of class `diffnet` and `data.frame`. The first column contains the sender, the second column the receiver node. The third column contains the improvement in fit from adding the edge that is represented by the row. The output additionally has the following attributes:

- `"diffusion_model"`: The diffusion model used to infer the diffusion network.
- `"diffusion_model_parameters"`: The parameters for the model that have been inferred by the approximate profile MLE procedure.

If the argument `trees` is set to `TRUE`, the output is a list with the first element being the `data.frame` described above, and the second element being the trees in edge-list form in a single `data.frame`.

## References

M. Gomez-Rodriguez, J. Leskovec, A. Krause. Inferring Networks of Diffusion and Influence. The 16th ACM SIGKDD Conference on Knowledge Discovery and Data Mining (KDD), 2010.

## Examples

```
# Data already in cascades format:
data(cascades)
out <- netinf(cascades, trans_mod = "exponential", n_edges = 5, params = 1)

# Starting with a dataframe
df <- simulate_rnd_cascades(10, n_nodes = 20)
cascades2 <- as_cascade_long(df, node_names = unique(df$node_name))
out <- netinf(cascades2, trans_mod = "exponential", n_edges = 5, params = 1)
```

## Description

This package provides an R implementation of the `netinf` algorithm created by Gomez Rodriguez, Leskovec, and Krause (2010). Given a set of events that spread between a set of nodes the algorithm infers the most likely stable diffusion network that is underlying the diffusion process.

**Details**

The package provides three groups of functions: 1) data preparation 2) estimation and 3) interpretation.

**Data preparation**

The core estimation function `netinf` requires an object of class `cascade` (see `as_cascade_long` and `as_cascade_wide`). Cascade data contains information on the potential nodes in the network as well as on event times for each node in each cascade.

**Estimation**

Diffusion networks are estimated using the `netinf` function. It produces a diffusion network in form of an edgelist (of class `data.frame`).

**Interpretation and Visualization**

Cascade data can be visualized with the `plot` method of the `cascade` class (`diffnet`, `plot.cascade`). Results of the estimation process can be visualized using the plotting method of the `diffnet` class.

**Performance**

If higher performance is required and for very large data sets, a faster pure C++ implementation is available in the Stanford Network Analysis Project (SNAP). The software can be downloaded at <http://snap.stanford.edu/netinf/>.

---

plot.cascade	<i>Plot a cascade object</i>
--------------	------------------------------

---

**Description**

Allows plotting of one or multiple, labeled or unlabeled cascades.

**Usage**

```
## S3 method for class 'cascade'
plot(x, label_nodes = TRUE, selection = NULL, ...)
```

**Arguments**

<code>x</code>	object of class <code>cascade</code> to be plotted.
<code>label_nodes</code>	logical, indicating if should the nodes in each cascade be labeled. If the cascades are very dense setting this to <code>FALSE</code> is recommended.
<code>selection</code>	a vector of cascade ids to plot.
<code>...</code>	additional arguments passed to plot.

**Details**

The function returns a ggplot plot object (class gg, ggplot) which can be modified like any other ggplot. See the ggplot documentation and the examples below for more details.

**Value**

A ggplot plot object.

**Examples**

```
data(cascades)
plot(cascades, selection = names(cascades$cascade_nodes)[1:5])
plot(cascades, label_nodes = FALSE, selection = sample(1:54, 20))

# Modify resulting ggplot object
library(ggplot2)
p <- plot(cascades, label_nodes = FALSE, selection = sample(1:54, 20))
## Add a title
p <- p + ggtitle('Your Title')
p
## Change Axis
p <- p + xlab("Your modified y axis label") #x and y labels are flipped here
p <- p + ylab("Your modified x axis label") #x and y labels are flipped here
p
```

---

plot.diffnet

*Visualize netinf output*


---

**Description**

Visualize the inferred diffusion network or the marginal gain in fit obtained by addition of each edge.

**Usage**

```
## S3 method for class 'diffnet'
plot(x, type = "network", ...)
```

**Arguments**

x	object of class diffnet to be plotted.
type	character, one of c("network", "improvement", "p-value") indicating if the inferred diffusion network, the improvement for each edge or the p-value from the vuong test for each edge should be visualized .
...	additional arguments.

**Details**

If 'type = improvement' a ggplot object is returned. It can be modified like any other ggplot. See the ggplot documentation and the examples in [plot.cascade](#).

**Value**

A ggplot plot object if type = "improvement" otherwise an igraph plot.

**Examples**

```
## Not run:
data(cascades)
res <- netinf(cascades, quiet = TRUE)
plot(res, type = "network")
plot(res, type = "improvement")
plot(res, type = "p-value")

## End(Not run)
```

---

policies

*US State Policy Adoption (SPID)*

---

**Description**

The SPID data includes information on the year of adoption for over 700 policies in the American states.

**Usage**

```
data(policies)
```

**Format**

The data comes in two objects of class `data.frame`. The first object, named `policies` contains the adoption events. Each row corresponds to an adoption event. Each adoption event is described by the three columns:

- `statenam`: Name of the adopting state.
- `policy`: Name of the policy.
- `adopt_year`: Year when the state adopted the policy.

The second object (`policies_metadata`) contains more details on each of the policies. It contains these columns:

- `policy`: Name of the policy.
- `source`: Original source of the data.
- `first_year`: First year any state adopted this policy.

- last\_year: Last year any state adopted this policy.
- adopt\_count: Number of states that adopted this policy.
- description: Description of the policy.
- majortopic: Topic group the policy belongs to.

Both data.frame objects can be joined (merged) on the common column policy (see example code).

### Details

This version 1.0 of the database. For each policy we document the year of first adoption for each state. Adoption dates range from 1691 to 2017 and includes all fifty states. Policies are adopted by anywhere from 1 to 50 states, with an average of 24 adoptions. The data were assembled from a variety of sources, including academic publications and policy advocacy/information groups. Policies were coded according to the Policy Agendas Project major topic code. Additional information on policies is available at the source repository.

### Source

<https://doi.org/10.7910/DVN/CVYSR7>

### References

Boehmke, Frederick J.; Mark Brockway; Bruce A. Desmarais; Jeffrey J. Harden; Scott LaCombe; Fridolin Linder; and Hanna Wallach. 2018. "A New Database for Inferring Public Policy Innovativeness and Diffusion Networks." Working paper.

### Examples

```
data('policies')

# Join the adoption events with the metadata
merged_policies <- merge(policies, policies_metadata, by = 'policy')
```

---

simulate_cascades	<i>Simulate cascades from a diffusion network</i>
-------------------	---

---

### Description

Simulate diffusion cascades based on the generative model underlying netinf and a diffusion network.

### Usage

```
simulate_cascades(diffnet, nsim = 1, max_time = Inf,
  start_probabilities = NULL, partial_cascade = NULL, params = NULL,
  model = NULL, nodes = NULL)
```

**Arguments**

diffnet	object of class diffnet.
nsim	integer, number of cascades to simulate.
max_time	numeric, the maximum time after which observations are censored
start_probabilities	a vector of probabilities for each node in diffnet, to be the node with the first event. If NULL a node is drawn from a uniform distribution over all nodes.
partial_cascade	object of type cascade, containing one partial cascades for which further development should be simulated.
params	numeric, (optional) parameters for diffusion time distribution. See the details section of <a href="#">netinf</a> for specification details. Only use this argument if parameters different from those contained in the diffnet object should be used or the network is not an object of class diffnet.
model	character, diffusion model to use. One of c("exponential", "rayleigh", "log-normal"). Only use this argument if parameters different from those contained in the diffnet object should be used or the network is not an object of class diffnet.
nodes	vector of node ids if different from nodes included in diffnet

**Value**

A data frame with three columns. Containing 1) The names of the nodes ("node\_name") that experience an event in each cascade, 2) the event time ("event\_time") of the corresponding node, 3) the cascade identifier "cascade\_id".

**Examples**

```
data(cascades)
out <- netinf(cascades, trans_mod = "exponential", n_edges = 5, params = 1)
simulated_cascades <- simulate_cascades(out, nsim = 10)

# Simulation from partial cascade
```

---

simulate\_rnd\_cascades *Simulate a set of random cascades*

---

**Description**

Simulate random cascades, for testing and demonstration purposes. No actual diffusion model is underlying these cascades.

**Usage**

```
simulate_rnd_cascades(n_cascades, n_nodes)
```

**Arguments**

`n_cascades`      Number of cascades to generate.  
`n_nodes`          Number of nodes in the system.

**Value**

A data frame containing (in order of columns) node ids, event time and cascade identifier.

**Examples**

```
df <- simulate_rnd_cascades(10, n_nodes = 20)
head(df)
```

---

`sim_validation`      *Larger simulated validation network.*

---

**Description**

A network from simulated data. For testing purposes.

**Usage**

```
data(sim_validation)
```

**Format**

An object of class `data.frame` with 4 columns, containing:

**origin\_node**      Origin of diffusion edge.  
**destination\_node**      Destination node of diffusion edge.  
**improvement**      Improvement in score for the edge  
**p-value**          p-value for vuong test

**Source**

See code below.



---

subset_cascade	<i>Select a subset of cascades from cascade object</i>
----------------	--

---

**Description**

Select a subset of cascades from cascade object

**Usage**

```
subset_cascade(cascade, selection)
```

**Arguments**

cascade	cascade, object to select from
selection	character or integer, vector of cascade_ids to select

**Value**

An object of class cascade containing just the selected cascades

**Examples**

```
data(policies)
cascades <- as_cascade_long(policies, cascade_node_name = 'statenam',
                           event_time = 'adopt_year', cascade_id = 'policy')
cascade_names <- names(cascades$cascade_times)
subset_cascade(cascades, selection = cascade_names[1:10])
```

---

subset_cascade_time	<i>Subset a cascade object in time</i>
---------------------	--

---

**Description**

Remove each all events occurring outside the desired subset for each cascade in a cascade object.

**Usage**

```
subset_cascade_time(cascade, start_time, end_time, drop = TRUE)
```

**Arguments**

cascade	cascade, object to subset.
start_time	numeric, start time of the subset.
end_time	numeric, end time of the subset.
drop	logical, should empty sub-cascades be dropped?

**Value**

An object of class `cascade`, where only events are included that have times `start_time <= t < end_time`.

**Examples**

```
data(cascades)
sub_cascades <- subset_cascade_time(cascades, 10, 20, drop=TRUE)
```

---

<code>summary.cascade</code>	<i>Summarize a cascade object</i>
------------------------------	-----------------------------------

---

**Description**

Generates summary statistics for single cascades and across cascades in a collection, contained in a `cascades` object.

**Usage**

```
## S3 method for class 'cascade'
summary(object, quiet = FALSE, ...)
```

**Arguments**

<code>object</code>	object of class <code>cascade</code> to be summarized.
<code>quiet</code>	logical, if <code>FALSE</code> summary stats are printed to std out.
<code>...</code>	Additional arguments passed to <code>summary</code> .

**Value**

Prints cascade summary information to the screen (if `quiet = FALSE`). `'# cascades'` is the number of cascades in the object, `'# nodes'` is the number of nodes in the system (nodes that can theoretically experience an event), `'# nodes in cascades'` is the number of unique nodes of the system that experienced an event and `'# possible edges'` is the number of edges that are possible given the cascade data (see [count\\_possible\\_edges](#) for details.).

Additional summaries for each cascade are returned invisibly. `cascade`, `length` (length of the cascade as an integer of how many nodes experienced and event) and `n_ties` (number of tied event times per cascade).

**Examples**

```
data(cascades)
summary(cascades)
```

---

validation

*Validation output from netinf source.*

---

### Description

Contains output from original netinf C++ implementation, executed on [cascades](#). For testing purposes.

### Usage

```
data(validation)
```

### Format

An object of class `data.frame` with 6 columns, containing:

**origin\_node** Origin of diffusion edge.

**destination\_node** Destination node of diffusion edge.

**volume** ??

**marginal\_gain** Marginal gain from edge.

**median\_time\_difference** Median time between events in origin and destination

**mean\_time\_difference** Mean time between events in origin and destination

### Source

Output from netinf example program (<https://github.com/snap-stanford/snap/tree/master/examples/netinf>).

# Index

## \* datasets

- cascades, [6](#)
- policies, [13](#)
- sim\_validation, [16](#)
- validation, [19](#)

- as.data.frame.cascade, [2](#)
- as.matrix.cascade, [3](#)
- as\_cascade\_long, [4](#), [9](#), [11](#)
- as\_cascade\_wide, [5](#), [9](#), [11](#)

- cascades, [6](#), [19](#)
- count\_possible\_edges, [6](#), [18](#)

- data.frame, [2](#), [4](#), [5](#), [10](#), [11](#)
- drop\_nodes, [7](#)

- is.cascade, [8](#)
- is.diffnet, [8](#)

- matrix, [3](#), [5](#)

- netinf, [8](#), [9](#), [11](#), [15](#)
- NetworkInference, [10](#)

- plot.cascade, [11](#), [11](#), [13](#)
- plot.diffnet, [12](#)
- policies, [13](#)
- policies\_metadata(policies), [13](#)

- sim\_validation, [16](#)
- simulate\_cascades, [14](#)
- simulate\_rnd\_cascades, [15](#)
- subset\_cascade, [17](#)
- subset\_cascade\_time, [17](#)
- summary.cascade, [18](#)

- validation, [19](#)